

Remainder Theorem: When a polynomial $f(x)$ is divided by $x-a$, the remainder is $f(a)$

$$f(x) = 2x^3 + 3x^2 - 17x - 30$$

a.) $x-1$

$a=1$

$$2(1)^3 + 3(1)^2 - 17(1) - 30$$

$$= -42$$

b.) $x-3$

$a=3$

$$2(3)^3 + 3(3)^2 - 17(3) - 30$$

Remainder = 0

Factor Theorem: If $x=a$ is substituted into a polynomial for x and the remainder is 0, then $x-a$ is a factor of the polynomial.

$$f(x) = 2x^3 + 3x^2 - 17x - 30$$

$$2(3)^3 + 3(3)^2 - 17(3) - 30 = 0$$

$$\text{Factor } \ominus = (x-3)$$

$$\text{Divide } \frac{2x^3 + 3x^2 - 17x - 30}{x-3}$$

$$\begin{array}{r|rrrr} 3 & 2 & 3 & -17 & -30 \\ & \downarrow & 6 & 27 & 30 \\ \hline & 2 & 9 & 10 & 0 \end{array}$$

$$(x-3)(2x^2 + 9x + 10) \rightarrow \text{factor}$$

$$(x-3)(2x+5)(x+2)$$